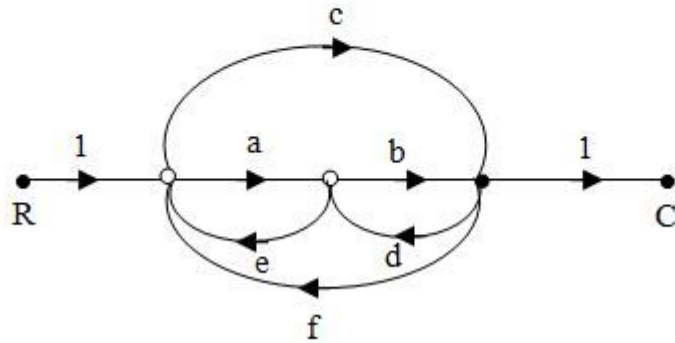


Question No: 1

Analysis

In the following signal flow graph, the number of individual loops is _____.



Not Attempted -- Correct Answer : 5 & Valid Answer Range :5,5

Video Solution

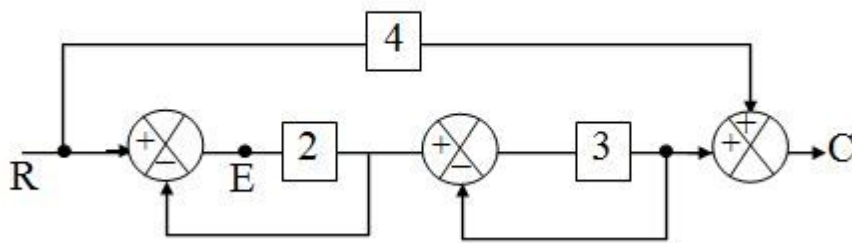
Solution :

Individual loop gains $L_1 = ae$, $L_2 = bd$, $L_3 = cde$, $L_4 = abf$, $L_5 = fc$

Question No: 2

Analysis

In the block diagram given below. The gain from R to E is _____.



Not Attempted -- Correct Answer : 0.33 & Valid Answer Range :0.3,0.4

Video Solution

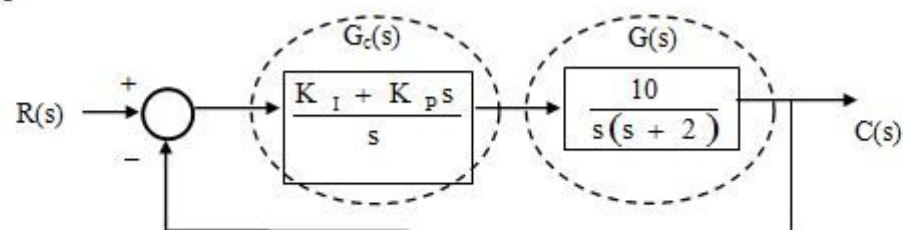
Solution :

$$\frac{E}{R} = \frac{1[1 - (-3)]}{1 - [-2 - 3] + [-2 \times -3]} = \frac{4}{12} = \frac{1}{3} = 0.33$$

Question No: 3

Analysis

Open loop transfer function $G(s)$ with compensator $G_c(s)$ is shown in figure



The closed loop system is stable when

(A) $K_p = \frac{K_I}{2}$

(B) $K_p < \frac{K_I}{2}$

(C) $K_p > \frac{K_I}{2}$

(D) $K_p = K_I$

Not Attempted -- Correct Answer : C

Solution :

$$C.E = s^3 + 2s^2 + 10K_p s + 10K_I = 0$$

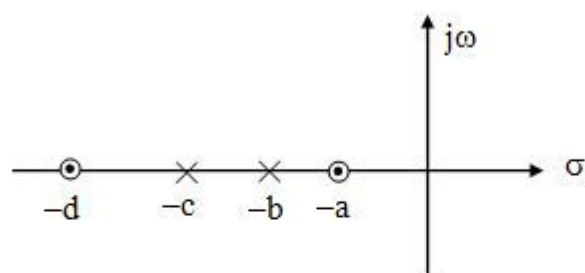
$$20K_p > 10K_I$$

$$K_p > K_I / 2$$

Question No: 4

Analysis

The pole zero plot of Lead - lag compensator is given below



The system will work as lag-lead compensator when

(A) $a > b, c > d$

(B) $a = b, c = d$

(C) $a < b, c < d$

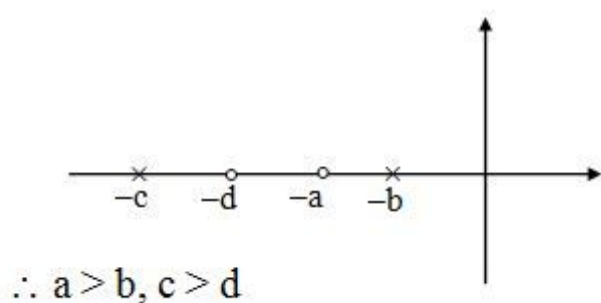
(D) $a > b > c > d$

Not Attempted -- Correct Answer : A

Video Solution

Solution :

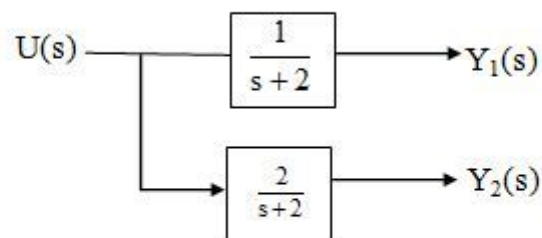
Lag – Lead compensator pole –zero pattern is



Question No: 5

Analysis

The block diagram of the system is



The number of state variables required to represent this state variable representation form is _____.

Not Attempted -- Correct Answer : 1 & Valid Answer Range : 1,1

Video Solution

Solution :

$$Y_1(s) = \frac{U(s)}{s+2}$$

$$Y_2(s) = \frac{2U(s)}{s+2}$$

$$\text{Let } Y_1 = X_1$$

$$Y_2 = 2X_1$$

$$X_1(s) = \frac{U(s)}{s+2}$$

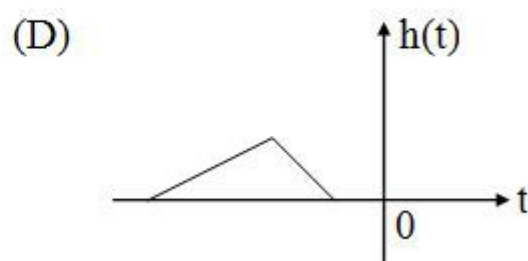
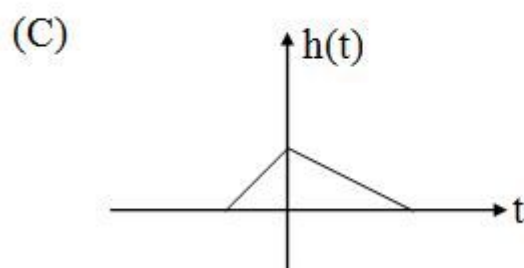
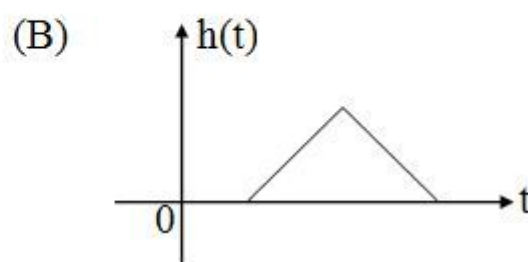
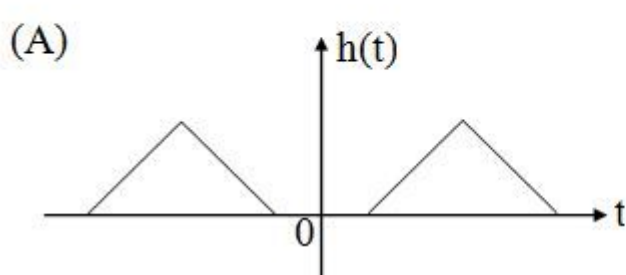
$$\dot{x}_1 = -2x_1 + u(t)$$

∴ In state variable conversion only 1 variable is required

Question No: 6

Analysis

Which of the following can be impulse response of causal system?



Not Attempted -- Correct Answer : B

Video Solution

Solution :

A system is said to be causal if $h(t) = 0$ for $t < 0$.

Option (B) is satisfying this condition. So, it is a causal system.

Question No: 7

Analysis

The unilateral Laplace transform of $f(t)$ is $\frac{1}{s^2 + 1}$.

The unilateral Laplace transform of $t^2 f(t)$ is

(A) $-\frac{s}{(s^2 + s + 1)^3}$

(B) $-\frac{2s + 1}{(s^2 + s + 1)^4}$

(C) $\frac{-3s^2 + 1}{(s^2 + 1)^3}$

(D) $\frac{6s^2 - 2}{(s^2 + 1)^3}$

Not Attempted -- Correct Answer : D

Video Solution

Solution :

$$f(t) \xrightarrow{LT} F(s) = \frac{1}{s^2 + 1}$$

$$t^2 f(t) \xrightarrow{LT} \frac{d^2}{ds^2} F(s) = \frac{6s^2 - 2}{(s^2 + 1)^3}$$

Question No: 8

Analysis

Consider signal $x(t) = \begin{cases} 1, & |t| \leq 2 \\ 0, & |t| > 2 \end{cases}$. Let $\delta(t)$ denote the unit impulse

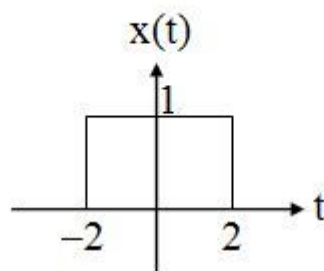
(Dirac-delta) function. The value of the integral $\int_0^5 2x(t-3)\delta(t-4) dt$

is _____.

Not Attempted -- Correct Answer : 2 & Valid Answer Range : 2,2

Solution :

Given,



From sifting property $\int_{t_1}^{t_2} x(t)\delta(t-t_0)dt = x(t_0) \quad t_1 \leq t_0 \leq t_2$

$= 0 \quad \text{otherwise}$

$$\int_0^5 2x(t-3)\delta(t-4) dt = 2x(4-3) = 2x(1) = 2 \times 1 = 2$$

Question No: 9

Analysis

Consider the discrete – time signal $x(n) = \left(\frac{1}{3}\right)^n u(n)$,

where $u(n) = \begin{cases} 1, & n \geq 0. \\ 0, & n < 0 \end{cases}$.

Define the signal $y(n)$ as $y(n) = x(-n)$. Then $\sum_{n=-\infty}^{\infty} y(n)$ equals to

Not Attempted -- Correct Answer : 1.5 & Valid Answer Range : 1.5,1.5

Video Solution

Solution :

Given $x(n) = \left(\frac{1}{3}\right)^n u(n)$ and $y(n) = x(-n)$.

$$\begin{aligned} \sum_{n=-\infty}^{\infty} y(n) &= \sum_{n=-\infty}^{\infty} \left(\frac{1}{3}\right)^{-n} u(-n) \\ &= \sum_{n=-\infty}^0 \left(\frac{1}{3}\right)^{-n} = 1 + \frac{1}{3} + \frac{1}{3^2} + \frac{1}{3^3} + \dots \\ &= \frac{\text{First term}}{1 - \text{Common ratio}} \\ &= \frac{1}{1 - \frac{1}{3}} = \frac{3}{2} \end{aligned}$$

Question No: 10

Analysis

The Fourier transform of $x(t) = e^{-at}u(-t)$, where $u(t)$ is the unit step function,

- (A) exists for any real value of 'a'
- (B) does not exists for any real value of 'a'
- (C) exists if the real value of 'a' is strictly negative
- (D) exists if the real value of 'a' is strictly positive

Not Attempted -- Correct Answer : C

Solution :

Given $x(t) = e^{-at} u(-t)$

Dirichlet's condition for convergence of Fourier transform is

$$\begin{aligned} \int_{-\infty}^{\infty} |x(t)| dt &< \infty \\ \int_{-\infty}^{\infty} |x(t)| dt &= \int_{-\infty}^0 e^{-at} dt < \infty \text{ only if } \text{Re}(a) < 0 \end{aligned}$$

Section Title : Two Marks Questions

Total Questions: 20

Max Marks : 2

-ve Marks :0.66

Question No: 11

Analysis

The characteristic equation of a system is given as $s^3 + 9s^2 + 4s + k = 0$;

If the system is marginally stable the values of k and undamped natural frequency ω_n respectively

(A) 36, 2 rad/sec

(B) 36, 4 rad/sec

(C) 18, 2 rad/sec

(D) 18, 4 rad/sec

Not Attempted -- Correct Answer : A

Video Solution

Solution :

$$\begin{array}{r|rr} s^3 & 1 & 4 \\ s^2 & 9 & k \\ s^1 & \frac{36-k}{9} & \\ s^0 & k & \end{array}$$

For marginally stable system

$$\frac{36-k}{9} = 0 \Rightarrow k = 36$$

Auxiliary equation $A(s) = 9s^2 + k = 0$

$$9s^2 + 36 = 0$$

$$s = \pm 2j$$

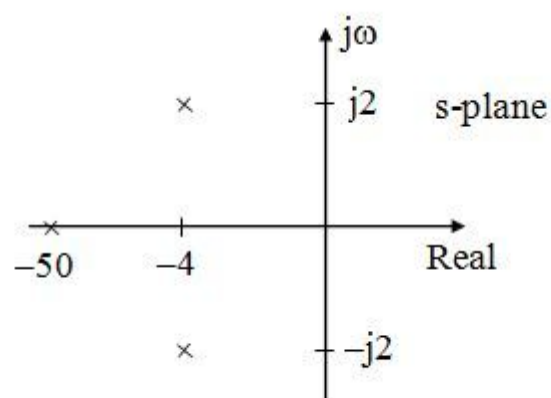
$$\omega_n = 2 \text{ rad/sec}$$

Question No: 12

Analysis

The closed loop poles of a system are shown in figure below.

The time taken to settle with in 2 % of tolerance is _____ (in sec)



Not Attempted -- Correct Answer : 1 & Valid Answer Range : 1,1

Solution :

Characteristic equation:

$$(s+5)(s+4-2j)(s+4+2j) = 0$$

Using dominate pole approximation

$$\approx (s+4-2j)(s+4+2j) = 0$$

$$(s+4)^2 + 4 = 0$$

$$s^2 + 8s + 20 = 0 \equiv s^2 + 2\zeta\omega_n s + \omega_n^2 = 0$$

$$\therefore \zeta\omega_n = 4$$

$$\therefore t_s(2\% \text{ tolerance}) = \frac{4}{\zeta\omega_n} = \frac{4}{4} = 1 \text{ sec}$$

Question No: 13

Analysis

Given CLTF $\frac{C(s)}{R(s)} = \frac{20s^2}{(s+1)(s+3)(s+5)}$; The natural response of the

system output when excited with an input of $(1+2t+3\frac{t^2}{2})u(t)$ is

(A) $-5e^{-t} + 10e^{-3t} - 9e^{-5t}$

(B) $5e^{-t} + 10e^{-3t} - 9e^{-5t}$

(C) $5e^{-t} + 10e^{-3t} + 9e^{-5t}$

(D) $-10e^{-t} + 10e^{-3t} - 9e^{-5t}$

Not Attempted -- Correct Answer : A

Video Solution

Solution :

$$r(t) = \left(1 + 2t + 3\frac{t^2}{2}\right)u(t) \rightarrow R(s) = \frac{1}{s} + \frac{2}{s^2} + \frac{3}{s^3}$$

$$C(s) = \frac{20s^2}{(s+1)(s+5)(s+3)} \cdot \left(\frac{1}{s} + \frac{2}{s^2} + \frac{3}{s^3}\right)$$

$$\Rightarrow C(s) = \frac{20(s^2 + 2s + 3)}{s(s+1)(s+5)(s+3)}$$

$$\Rightarrow C(s) = \frac{4}{s} - \frac{5}{s+1} + \frac{10}{s+3} - \frac{9}{s+5}$$

$$L^{-1}[C(s)] = c(t) = 4 - 5e^{-t} + 10e^{-3t} - 9e^{-5t}$$

The natural response (or) transient response component can be given

as

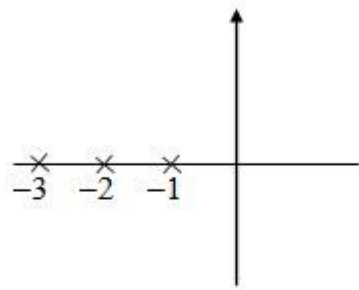
$$[c(t)]_{\text{natural}} = -5e^{-t} + 10e^{-3t} - 9e^{-5t}$$

Question No: 14

Analysis

A system is described by the state equation $\dot{X} = AX + BU$.

The output is given by $Y = CX$. The system poles are given as shown in figure below



The state space representation corresponding matrix “A” is

(A) $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$

(B) $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 6 & 11 & 6 \end{bmatrix}$

(C) $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ -6 & -11 & -6 \end{bmatrix}$

(D) $\begin{bmatrix} 1 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$

Not Attempted -- Correct Answer : A

Video Solution

Solution :

$$TF = \frac{k}{(s+1)(s+2)(s+3)} = \frac{k}{s^3 + 6s^2 + 11s + 6}$$

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}$$

Question No: 15

Analysis

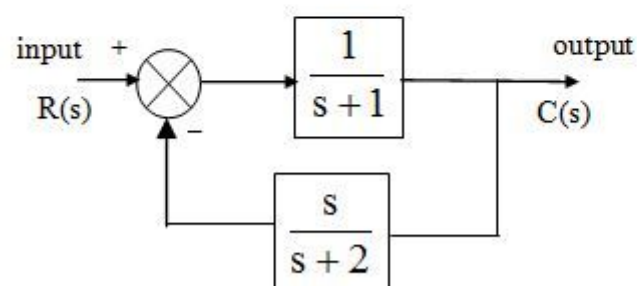
For the feedback control system shown in figure below, the sensitivity of overall gain with respect to feedback path gain is

(A) $\frac{-1}{s^2 + 4s + 2}$

(B) $\frac{-s}{s^2 + 4s + 2}$

(C) $\frac{s}{s^2 + 4s + 2}$

(D) $\frac{1}{s^2 + 4s + 2}$



Not Attempted -- Correct Answer : B

Solution :

$$\text{Let } M = \frac{G}{1+GH}$$

$$G = \frac{1}{s+1}, H = \frac{s}{s+2}$$

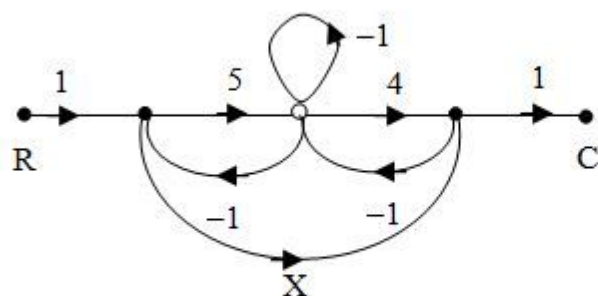
$$S_H^M = \frac{\partial M}{\partial H} \times \frac{H}{M} = \frac{-GH}{1+GH}$$

$$= \frac{-\frac{1}{s+1} \times \frac{s}{s+2}}{1 + \frac{1}{s+1} \times \frac{s}{s+2}} = - \left[\frac{s}{s^2 + 4s + 2} \right]$$

Question No: 16

Analysis

Consider the signal flow graph of a system is shown in figure below.



If the gain $\frac{C}{R}$ is 4 then the value of X is _____.

Not Attempted -- Correct Answer : 4 & Valid Answer Range :4,4

Video Solution

Solution :

Forward path gains = (1) (5) (4) (1) = 20

(1) (X) (1) = X

Loop gains = -5, -4 and -1, X

$$\frac{C}{R} = \frac{20 + X[1+1]}{1 - (-5 - 4 - 1 + X)} = \frac{20 + 2X}{11 - X}$$

$$\frac{20 + 2X}{11 - X} = 4$$

$$20 + 2X = 44 - 4X$$

$$6X = 24$$

$$X = 4$$

Question No: 17

Analysis

Closed loop transfer function of a unity feedback system is

$$\frac{k}{s^2 + 6s + 5 + k} \quad (k > 0).$$

Consider the points in the s-plane $s_1 = -3+j3$, $s_2 = -3-j4$ with respect to the root Loci diagram

- (A) s_1 is on the root loci diagram but not s_2
- (B) s_2 is on the root loci diagram but not s_1
- (C) both are on the root Loci diagram
- (D) both are not on the root Loci diagram

Not Attempted -- Correct Answer : C

Video Solution

Solution :

Characteristic equation = $1 + G(s)H(s) = 0$

$$s^2 + 6s + 5 + k = 0$$

$$1 + \frac{k}{(s^2 + 6s + 5)} = 0$$

$$\begin{aligned} G(s)H(s) &= \frac{k}{(s^2 + 6s + 5)} \\ &= \frac{k}{(s + 5)(s + 1)} \end{aligned}$$

$$\begin{aligned} \angle \frac{k}{(s + 5)(s + 1)} \bigg|_{\text{at } s = -3 + j3} \\ &= \angle \frac{k}{(-3 + j3 + 5)(-3 + j3 + 1)} \\ &= -(\tan^{-1} \frac{3}{2} + 180^\circ - \tan^{-1} \frac{3}{2}) \\ &= -180^\circ = -\pi \end{aligned}$$

Phase is equal to odd multiplier of π

$\therefore s_1$ is on root locus diagram.

$$\begin{aligned} \angle \frac{k}{(s + 5)(s + 1)} \bigg|_{\text{at } s = -3 - j4} \\ &= \angle \frac{k}{(-3 - j4 + 5)(-3 - j4 + 1)} \\ &= -[-\tan^{-1}(4/2) + 180^\circ + \tan^{-1}(4/2)] \\ &= -180^\circ \end{aligned}$$

Phase is equal to odd multiplier of π

$\therefore s_2$ is on root locus diagram

The point in the s-plane $s = -2$, to be lie on the root loci diagram of a system with loop transfer function $\frac{k}{s(s+4)(s+10)}$, the value 'k' is

- (A) 8 (B) 16
- (C) 32 (D) Such k value will not exist

Not Attempted -- Correct Answer : C

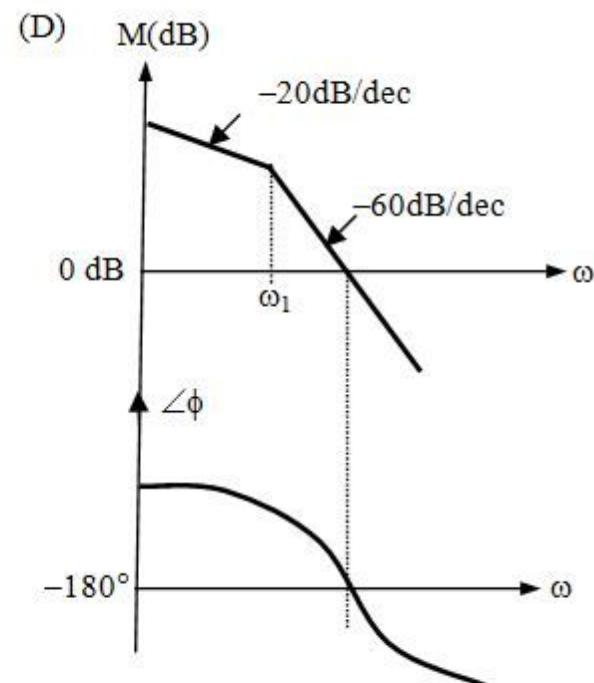
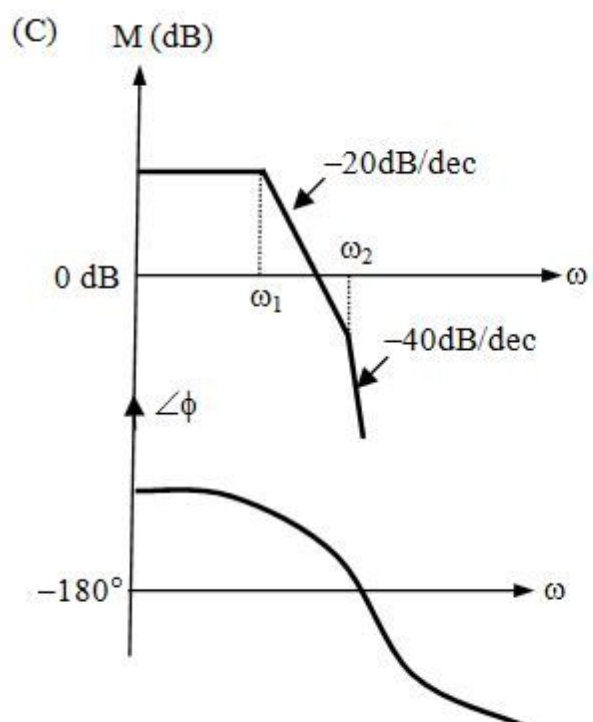
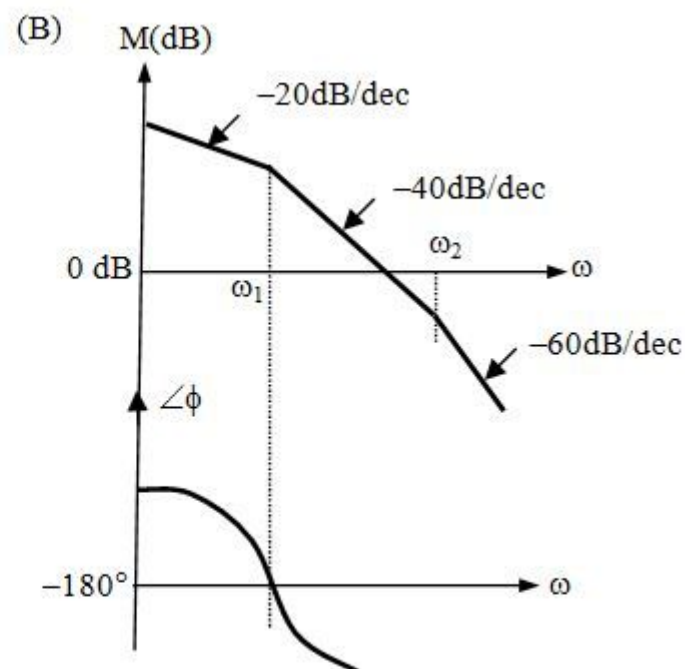
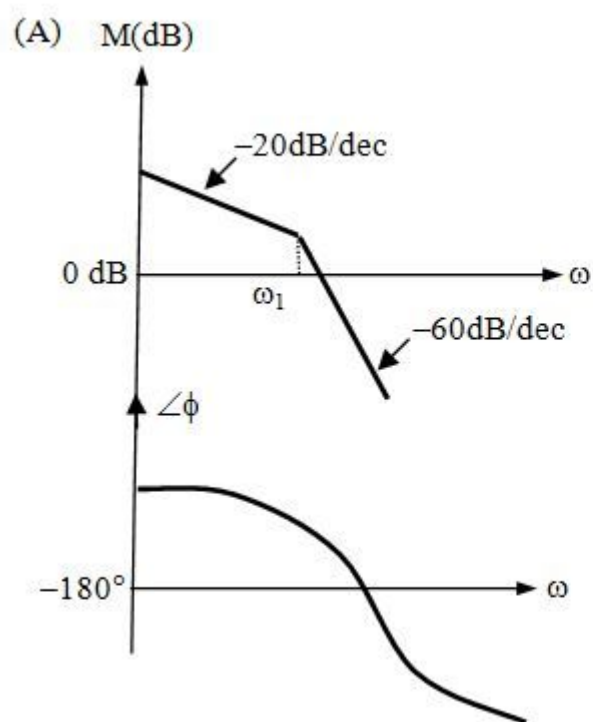
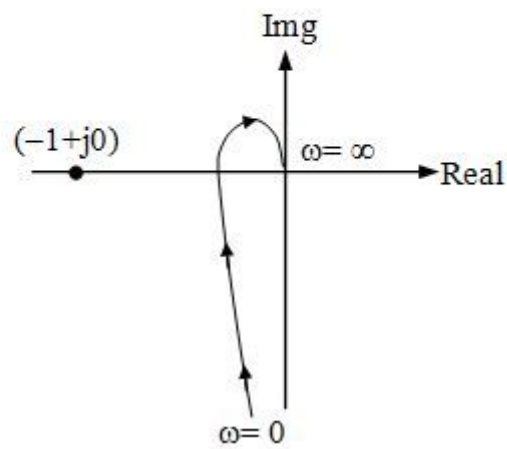
Solution :

$$\begin{aligned}k|_{s=-2} &= |s(s+4)(s+10)| \\&= |(-2)(-2+4)(-2+10)| \\&= |(2)(2)(8)| \\k &= 32\end{aligned}$$

Question No: 19

Analysis

The Nyquist plot for a control system over the frequency range $\omega = 0$ to $\omega = \infty$ is shown in figure. The Bode plot for the system will be



Not Attempted -- Correct Answer : A

Video Solution

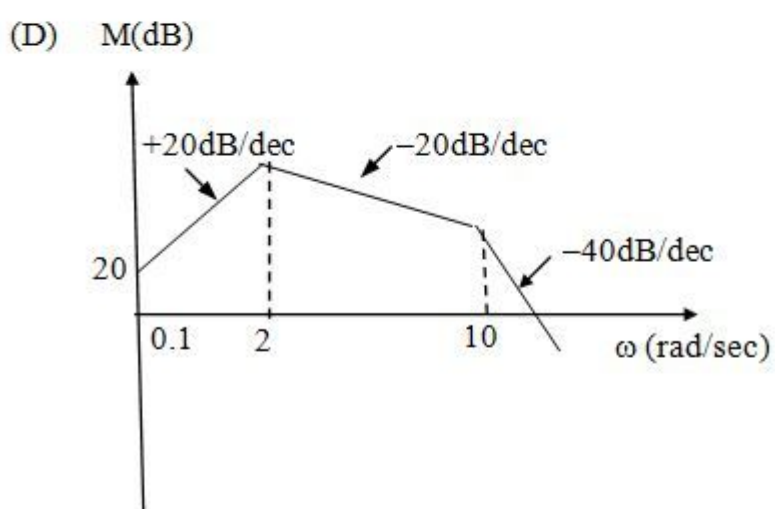
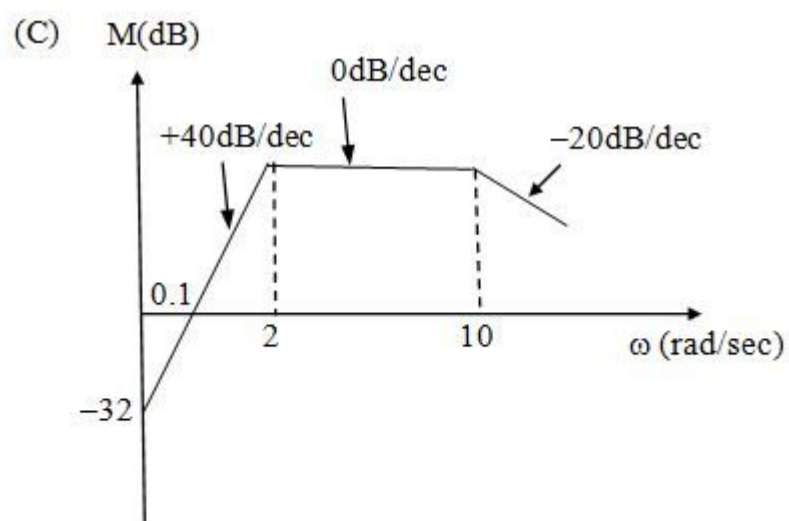
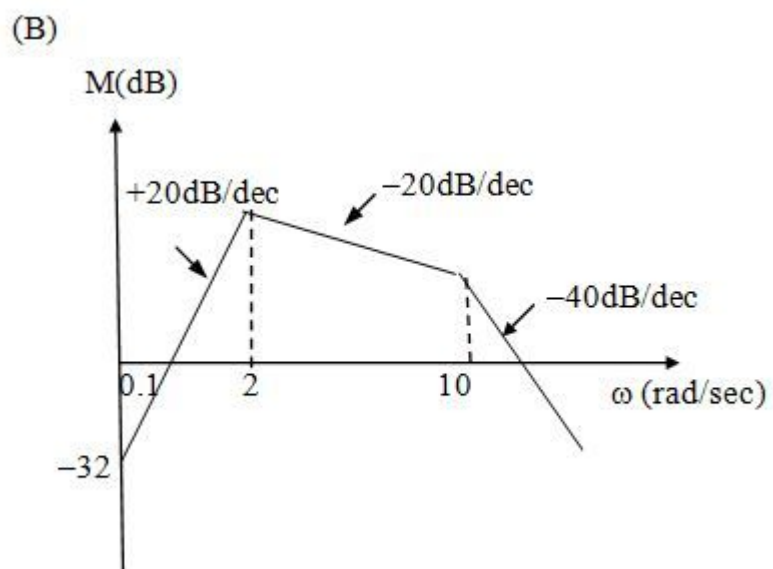
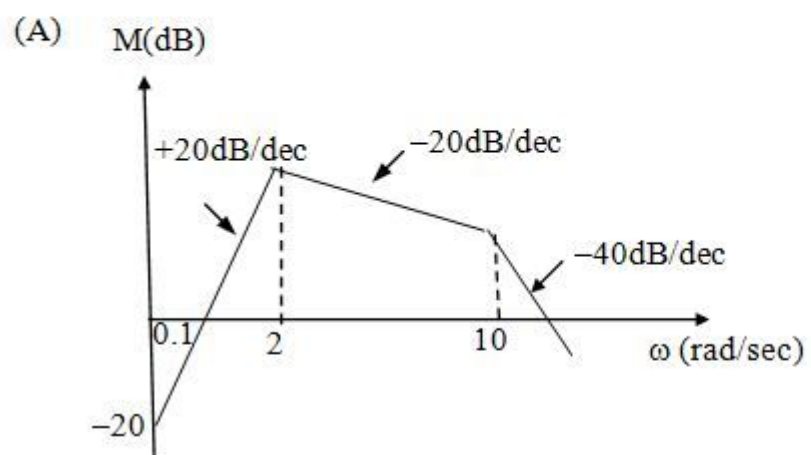
Solution :

The given polar plot is a stable system and having type is one.

That means initial slope of magnitude plot is -20dB/dec .

In option (A), $\omega_{PC} > \omega_{gc}$, the system is stable and having initial slope of -20dB/dec

The Bode magnitude plot of a system $G(s)H(s) = \frac{10se^{-2s}}{(s+2)^2(s+10)}$, is



Not Attempted -- Correct Answer : B
Solution :

$$G(s)H(s) = \frac{10se^{-2s}}{2^2 \times 10 \left(1 + \frac{s}{2}\right)^2 \left(1 + \frac{s}{10}\right)} = \frac{0.25(s)e^{-2s}}{\left(1 + \frac{s}{2}\right)^2 \left(1 + \frac{s}{10}\right)}$$

$$M|_{\omega=0.1} = 20 \log 0.25 + 20 \log 0.1 = -32 \text{ dB}$$

\Rightarrow One zero at origin \Rightarrow Initial slope is +20 dB/dec

At $\omega = 2$ rad/sec change in slope

$$= (+20 - 40) = -20 \text{ dB/dec}$$

At $\omega = 10$ rad/sec change in slope $= (-20 - 20) = -40 \text{ dB/dec}$

Question No: 21

Analysis

DFT of real sequence is given as

$X(k) = \{1, 2, a, b, 0, 1-j, -2, c\}$. Then the value of a, b, c respectively

(A) 2, $1-j$, -2

(B) 4, j, 1

(C) -2, $1+j$, 2

(D) -1, $1+j$, 2

Not Attempted -- Correct Answer : C

Video Solution

Solution :

We know that DFT of a real sequence has conjugate symmetry

$$\text{i.e, } X(k) = X^*(N-K)$$

$$\text{Given } N=8. X(k) = X^*(8-K)$$

$$a = X(2) = X^*(8-2) = X^*(6) = -2$$

$$b = X(3) = X^*(8-3) = X^*(5) = 1+j$$

$$c = X(7) = X^*(8-7) = X^*(1) = 2$$

Question No: 22

Analysis

$$\text{Let } x(n) = n^2 3^n u(n) \text{ and } x(n) \leftrightarrow X(z). \text{ If } Y(z) = \frac{z^2 - z^{-2}}{2} X(z).$$

Then $y(n)$ value at $n = 2$ is _____.

Not Attempted -- Correct Answer : 648 & Valid Answer Range : 648,648

Solution :

$$\text{Given } Y(z) = \frac{1}{2} z^2 X(z) - \frac{1}{2} z^{-2} X(z)$$

$$y(n) = \frac{1}{2} x(n+2) - \frac{1}{2} x(n-2)$$

$$y(n) = \frac{1}{2} (n+2)^2 3^{n+2} u(n+2) - \frac{1}{2} (n-2)^2 3^{n-2} u(n-2)$$

$$y(2) = \frac{1}{2} (2+2)^2 \cdot 3^4 \cdot 1 - \frac{1}{2} (2-2)^2 \cdot 3^{(2-2)} \cdot 1$$

$$= \frac{1}{2} \cdot 16 \cdot 81$$

$$= 8 \times 81$$

$$y(2) = 648$$

Question No: 23

Analysis

An LTI system is described by the difference equation

$$y(n) - \frac{5}{6} y(n-1) + \frac{1}{6} y(n-2) = x(n). \text{ If system is unstable and anti-}$$

causal then impulse response of the system is given by

$$(A) \ 3 \left(\frac{1}{2} \right)^n u(n-1) - 2 \left(\frac{1}{3} \right)^n u(-n-1)$$

$$(B) \ -3 \left(\frac{1}{2} \right)^n u(-n-1) - 2 \left(\frac{1}{3} \right)^n u(-n-1)$$

$$(C) \ 3 \left(\frac{1}{2} \right)^n u(-n-1) + 2 \left(\frac{1}{3} \right)^n u(-n-1)$$

$$(D) \ -3 \left(\frac{1}{2} \right)^n u(-n-1) + 2 \left(\frac{1}{3} \right)^n u(-n-1)$$

Not Attempted -- Correct Answer : D

Video Solution

Solution :

$$\text{Given } y(n) - \frac{5}{6}y(n-1) + \frac{1}{6}y(n-2) = x(n)$$

Taking Z transform then

$$Y(z) - \frac{5}{6}z^{-1}Y(z) + \frac{1}{6}Y(z)z^{-2} = X(z)$$

$$\therefore \frac{Y(z)}{X(z)} = \frac{1}{1 - \frac{5}{6}z^{-1} + \frac{1}{6}z^{-2}}$$

$$\therefore \frac{Y(z)}{X(z)} = \frac{3}{\left(1 - \frac{1}{2}z^{-1}\right)} - \frac{2}{\left(1 - \frac{1}{3}z^{-1}\right)}$$

Since $H(z)$ is given as anti-causal and unstable. So, ROC is $\therefore |z| < \frac{1}{3}$

$$h(n) = -3\left(\frac{1}{2}\right)^n u(-n-1) + 2\left(\frac{1}{3}\right)^n u(-n-1)$$

Question No: 24

Analysis

$$\text{Consider } X(s) = \frac{\frac{1}{4}}{\left(s^2 - \frac{s}{\sqrt{2}} + \frac{1}{4}\right)\left(s^2 + \frac{s}{\sqrt{2}} + \frac{1}{4}\right)} \text{ then } x(t) \text{ is}$$

(A) real and even

(B) imaginary and even

(C) real and odd

(D) data insufficient

Not Attempted -- Correct Answer : A

Solution :

$$\text{Given } X(s) = \frac{\frac{1}{4}}{\left(s^2 - \frac{s}{\sqrt{2}} + \frac{1}{4}\right)\left(s^2 + \frac{s}{\sqrt{2}} + \frac{1}{4}\right)}$$

$$X(s) = \frac{\frac{1}{4}}{\left(s - \frac{1}{2}e^{j\frac{\pi}{4}}\right)\left(s - \frac{1}{2}e^{-j\frac{\pi}{4}}\right)\left(s + \frac{1}{2}e^{-j\frac{\pi}{4}}\right)\left(s + \frac{1}{2}e^{j\frac{\pi}{4}}\right)}$$

Since poles are in complex conjugate hence $x(t)$ is real. Since poles are symmetric about $j\omega$ axis hence $x(t)$ is even

Question No: 25

Analysis

Consider $H(s) = \frac{b[s^2 + 4s + 3a]}{[s^2 + 3s + 4b]}$.

Let $x(t)$ is given as $u(t)$ and $y(0) = 2$, $y(\infty) = 10$.

Then $\left(\frac{a}{b}\right)$ is _____.

Not Attempted -- Correct Answer : 6.6 & Valid Answer Range : 6.5, 6.7

Video Solution

Solution :

$$Y(s) = X(s) H(s)$$

Given $x(t) = u(t) \Rightarrow X(s) = \frac{1}{s}$

$$Y(s) = \frac{1}{s} \frac{b[s^2 + 4s + 3a]}{[s^2 + 3s + 4b]}$$

Given $y(0) = 2$

From initial value theorem $y(0) = \lim_{s \rightarrow \infty} s Y(s) = 2$

$$\lim_{s \rightarrow \infty} \frac{s}{s} \frac{b[s^2 + 4s + 3a]}{[s^2 + 3s + 4b]} = 2$$

$$\lim_{s \rightarrow \infty} \frac{bs^2 \left[1 + \frac{4}{s} + \frac{3a}{s^2} \right]}{s^2 \left[1 + \frac{3}{s} + \frac{4b}{s^2} \right]} = 2$$

$$b = 2$$

Given $y(\infty) = 10$

From final value theorem $y(\infty) = \lim_{s \rightarrow 0} s Y(s) = 10$

$$\lim_{s \rightarrow 0} \frac{s}{s} \frac{b[s^2 + 4s + 3a]}{[s^2 + 3s + 4b]} = 10$$

$$\frac{b \cdot 3a}{4b} = 10$$

$$a = \frac{40}{3}$$

$$\frac{a}{b} = \frac{\frac{40}{3}}{\frac{2}{1}} = \frac{40}{6} = \frac{20}{3} = 6.6$$

Consider a system with input $x(t)$ and output $y(t)$ related as follows

$$y(t) = \frac{d}{dt} \{e^{-t} x(t)\}.$$

Which one of the following statements is true?

- (A) The system is nonlinear
- (B) The system is time – invariant
- (C) The system is stable
- (D) The system has memory

Not Attempted -- Correct Answer : D

Solution :

Given the system, $y(t) = \frac{d}{dt} \{e^{-t} x(t)\}$

$$y(t) = e^{-t} \frac{d}{dt} [x(t)] + [-x(t) e^{-t}] = e^{-t} \left[\frac{d}{dt} x(t) - x(t) \right]$$

As $y(t)$ is obtained from linear operations on $x(t)$, the system is linear.

As the input $x(t)$ is multiplied by a time varying function e^{-t} , the system is Time-varying.

For a bounded input $x(t)$,

$$x(t) = u(t)$$

$$\Rightarrow y(t) = e^{-t} \delta(t) - e^{-t} u(t)$$

$$\Rightarrow y(t) = \delta(t) - e^{-t} u(t)$$

$$\Rightarrow y(0) = \infty \text{ output is unbounded. Therefore the system is unstable.}$$

As $y(t)$ depends on $\frac{dx(t)}{dt}$, the system has memory.

Question No: 27

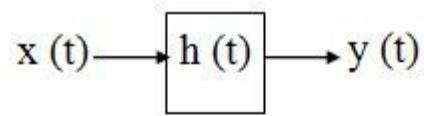
Analysis

The impulse response of a system is $h(t) = tu(t)$. For an input $u(t-1)$, the output is

- (A) $\frac{t^2}{2} u(t)$
- (B) $\frac{t(t-1)}{2} u(t-1)$
- (C) $\frac{(t-1)^2}{2} u(t-1)$
- (D) $\frac{t^2-1}{2} u(t-1)$

Not Attempted -- Correct Answer : C

Solution :



$$y(t) = x(t) * h(t) = u(t-1) * t u(t)$$

Apply laplace transform on both sides

$$Y(s) = \frac{e^{-s}}{s} \times \frac{1}{s^2} = \frac{e^{-s}}{s^3}$$

$$y(t) = \frac{1}{2} (t-1)^2 u(t-1)$$

Question No: 28

Analysis

Consider a discrete – time system for which the input $x(n]$ and the

output $y(n]$ are related as $y(n) = x(n) - \frac{1}{3} y(n-1)$. If $y(n) = 0$

for $n < 0$ and $x(n) = \delta(n)$, then $y(n]$ can be expressed in terms of the unit step $u(n)$ as

(A) $\left(-\frac{1}{3}\right)^n u(n)$

(B) $\left(\frac{1}{3}\right)^n u(n)$

(C) $(3)^n u(n)$

(D) $(-3)^n u(n)$

Not Attempted -- Correct Answer : A

Solution :

Given $y(n) = x(n) - \frac{1}{3} y(n-1)$, and $y(n) = 0$, $n < 0$

$$y(n) + \frac{1}{3} y(n-1) = x(n)$$

Apply z-transform on both sides

$$Y(z) \left[1 + \frac{1}{3} z^{-1} \right] = X(z)$$

$$H(z) = \frac{Y(z)}{X(z)} = \frac{1}{1 + \frac{1}{3} z^{-1}} = \frac{z}{z + \frac{1}{3}}$$

For the given $x(n) = \delta(n)$, $X(z) = 1$

$$\therefore Y(z) = \frac{z}{z + \frac{1}{3}}$$

Use the standard Z.T pair:

$$a^n u(n) \longrightarrow \frac{z}{z-a}, |z| > |a|$$

$$y(n) = \left(-\frac{1}{3}\right)^n u(n), |z| > \frac{1}{3}$$

Question No: 29

Analysis

Let $f(x)$ be a real, periodic function satisfying $f(-x) = -f(x)$.

The general form of its Fourier series representation would be

(A) $f(x) = a_0 + \sum_{k=1}^{\infty} a_k \cos(kx)$

(B) $f(x) = \sum_{k=1}^{\infty} b_k \sin(kx)$

(C) $f(x) = a_0 + \sum_{k=1}^{\infty} a_{2k} \cos(kx)$

(D) $f(x) = \sum_{k=0}^{\infty} a_{2k+1} \cos(2k+1)x$

Not Attempted -- Correct Answer : B

Video Solution

Solution :

Given $f(x)$ is an odd periodic function. So, cosine terms will be zero in trigonometric Fourier series.

$$\therefore f(x) = \sum_{k=1}^{\infty} b_k \sin(kx)$$

Question No: 30

Analysis

A sinusoid $x(t)$ of unknown frequency is sampled by an impulse train of period 20 ms. The resulting sample train is next applied to an ideal low pass filter with a cutoff at 25 Hz. The filter output is seen to be a sinusoid of frequency 20 Hz. This means that $x(t)$ has a frequency of

(A) 10 Hz

(B) 60 Hz

(C) 30 Hz

(D) 90 Hz

Not Attempted -- Correct Answer : C

Solution :

Given $T_s = 20 \text{ msec}$

$$f_s = \frac{1}{T_s} = \frac{1}{20 \times 10^{-3}} = \frac{1000}{20} = 50 \text{ Hz}$$

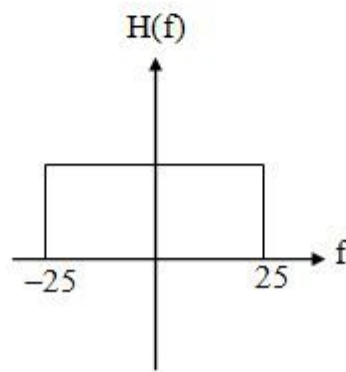
Assume the frequency of the input signal is ' f_m ' then

$$n = 0 \quad -f_m, f_m$$

$$n = 1 \quad f_s - f_m, f_s + f_m$$

$$n = 2 \quad 2f_s - f_m, 2f_s + f_m$$

The above frequencies are passed through an ideal low pass filter with a cutoff at 25Hz as shown in figure.



Consider 'a' option $f_m = 10$ then output frequencies are

$$= 10, -10, 40, 60, 90, 110 \dots \text{Output is 10 Hz}$$

Consider 'b' option: $f_m = 60 \text{ Hz}$ then output frequencies are $= 60, -60, -10, 110, 40, 160 \dots$ No output

Consider 'c' option: $f_m = 30 \text{ Hz}$ then output frequencies are $= 30, -30, 20, 80, 70, 130 \dots$ The output of low pass filter $= 20 \text{ Hz}$

Consider 'd' option: $f_m = 90 \text{ Hz}$ then output frequencies are $= 90, -90, -40, 140, 190, 10 \dots$ The output of low pass filter $= 10 \text{ Hz}$.

So, the right option is (C).